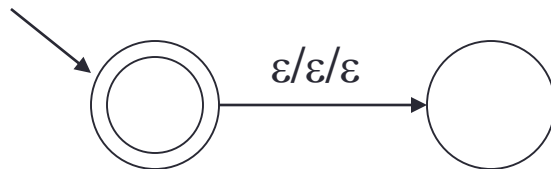


# Deterministic PDAs

A PDA  $M$  is **deterministic** iff:

- $\Delta_M$  contains no pairs of transitions that compete with each other, and
- Whenever  $M$  is in an accepting configuration it has no available moves.



$M$  can choose between accepting and taking the  $\epsilon$ -transition, so it is not deterministic.

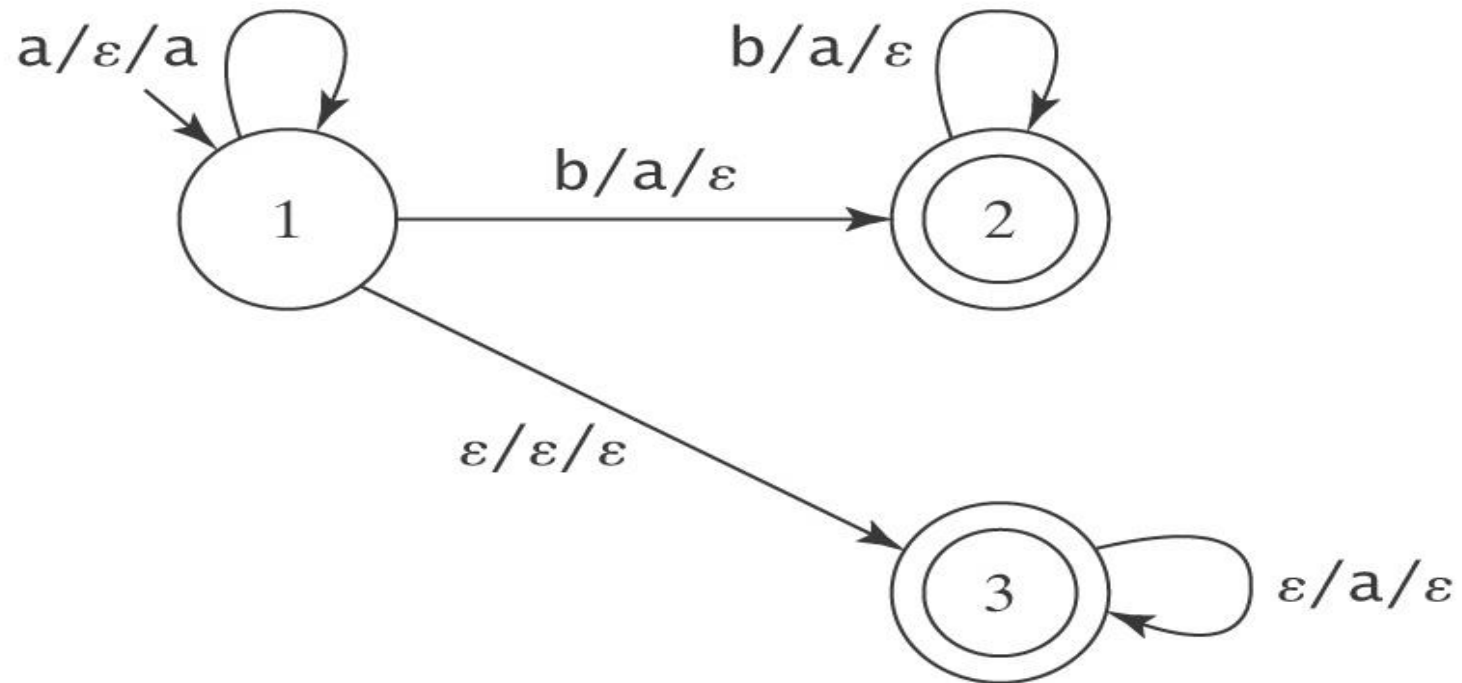
# Deterministic CFLs

A language  $L$  is **deterministic context-free** iff  $L\$$  can be accepted by some deterministic PDA.

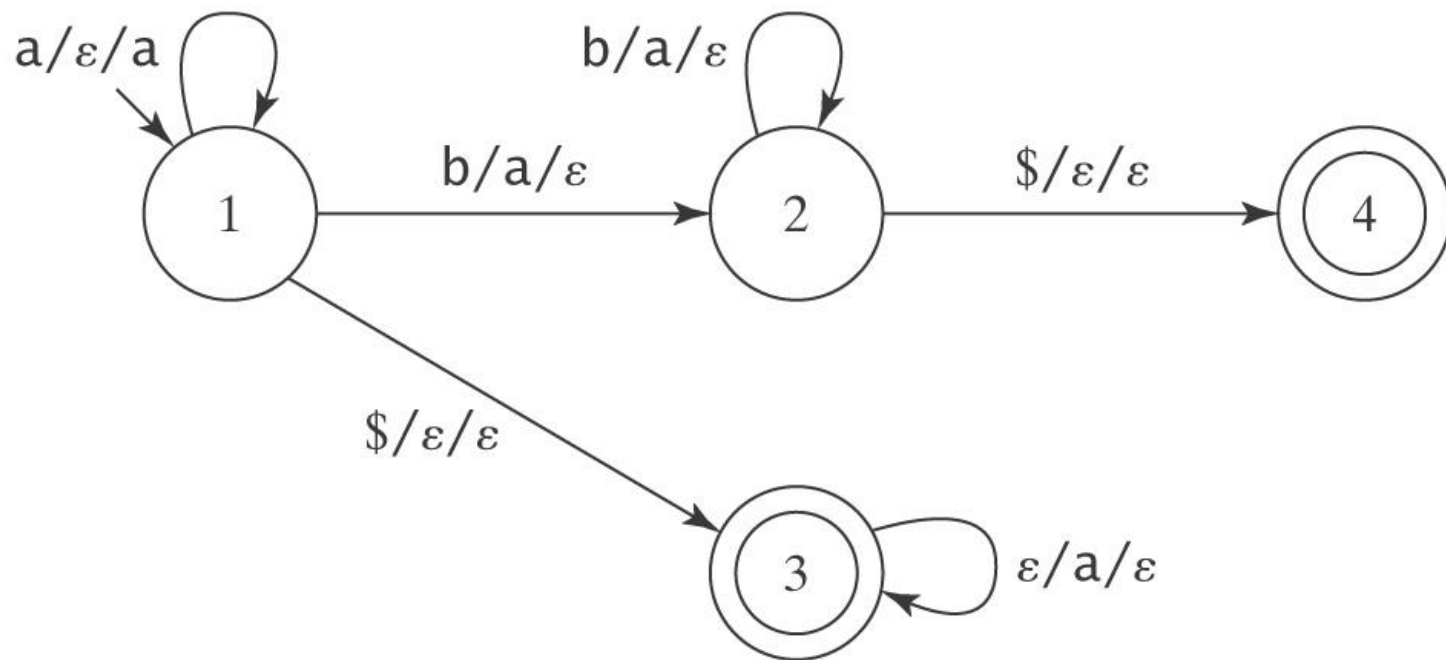
Why \$?

Let  $L = a^* \cup \{a^n b^n : n > 0\}$ .

An NDPDA for  $L = a^* \cup \{a^n b^n : n > 0\}$ .



An DPDA for  $L = a^* \cup \{a^n b^n : n > 0\}$ .



# Decision problems for DCFL

- The Deterministic CF Languages are Closed Under Complement
- DCFLs are Not Closed Under Union
- DCFLs are Not Closed Under Intersection

# Nondeterministic CFLs

**Theorem:** There exist CLFs that are not deterministic.

**Proof:** By example. Let  $L = \{a^i b^j c^k, i \neq j \text{ or } j \neq k\}$ .  $L$  is CF. If  $L$  is DCF then so is:

$$\begin{aligned} L' &= \neg L. \\ &= \{a^i b^j c^k, i, j, k \geq 0 \text{ and } i = j = k\} \cup \\ &\quad \{w \in \{a, b, c\}^* : \text{the letters are out of order}\}. \end{aligned}$$

But then so is:

$$\begin{aligned} L'' &= L' \cap a^* b^* c^*. \\ &= \{a^n b^n c^n, n \geq 0\}. \end{aligned}$$

But it isn't. So  $L$  is context-free but not deterministic context-free.

This simple fact poses a real problem for the designers of efficient context-free parsers.

# The CFL Hierarchy

